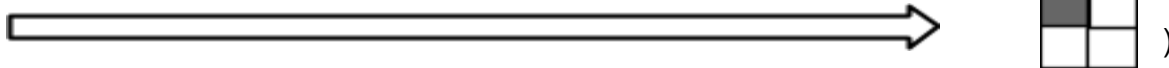


LEVEL 5 EXAMPLE

Problem of the Month Reflection: October

The last level I completed (as of October 27th) was Level B, which had to do with equivalent fractions. The problem explained that in a video game, there are doors labeled with cards. These cards all have different fractions on them, and the video character must pass through them ($\frac{6}{8}$, $\frac{4}{8}$, $\frac{6}{9}$, $\frac{16}{32}$, $\frac{21}{28}$, $\frac{12}{18}$, $\frac{6}{12}$, $\frac{6}{18}$). In order to pass through the doors, however, the character must place the cards in the correct pocket of his jacket, which are also labeled ($\frac{3}{6}$, $\frac{5}{15}$, $\frac{8}{12}$, $\frac{9}{12}$). I figured that the way to determine which cards went in which pockets was to find out which fractions were equivalent. Therefore, I simplified all of the fractions ($\frac{3}{6}=\frac{1}{2}$, $\frac{5}{15}=\frac{1}{3}$, $\frac{8}{12}=\frac{2}{3}$, and $\frac{9}{12}=\frac{3}{4}$ for the pockets and $\frac{6}{8}=\frac{3}{4}$, $\frac{4}{8}=\frac{1}{2}$, $\frac{6}{9}=\frac{2}{3}$, $\frac{16}{32}=\frac{1}{2}$, $\frac{21}{28}=\frac{3}{4}$, $\frac{12}{18}=\frac{2}{3}$, $\frac{6}{12}=\frac{1}{2}$, and $\frac{6}{18}=\frac{2}{6}=\frac{1}{3}$ for the doorways). Finally, because on the page the pockets were arranged so that two pockets were on the top half of a t-shirt and two were on the bottom, I drew a small box separated into four quadrants near each doorway illustration and colored in the quadrant in the same position the pocket it belonged in was.

(Example:



Once I had done that, I could easily “write a note” to the person playing the video game explaining which cards went where by referring to the first page on which I showed my work. Basically, the cards to doors $\frac{4}{8}$, $\frac{6}{12}$, and $\frac{16}{32}$ all belonged in the pocket marked $\frac{3}{6}$ because they all equaled $\frac{1}{2}$. In the pocket marked $\frac{5}{15}$, door $\frac{6}{18}$'s card belonged because both the fractions equaled $\frac{1}{3}$. The cards $\frac{6}{9}$, and $\frac{12}{16}$ should have gone into the pocket marked $\frac{8}{12}$, because they were all equal to $\frac{2}{3}$, and in the pocket labeled $\frac{9}{12}$, door cards $\frac{6}{8}$ and $\frac{21}{28}$ belonged because the three fractions were equivalent to $\frac{3}{4}$. Simply put, the cards belonged in the pockets they did because in each pocket, all the fractions were equivalent.

To solve this problem, I used my knowledge of fractions as well as division and multiplication. In order to simplify the fractions, I had to know multiples of certain numbers and understand that the same fraction can be written in many different ways-- a concept that might be hard at first, but one that once understood seems quite simple and is very valuable. I also had to know multiples of numbers such as 2, 3, 4, 5, 6, 8, 16, etc., in order to notice the pattern of equivalent fractions I spotted, which was what made me realize that equivalent fractions were the key to this problem.